SAMPLE PAPER 2014: PAPER 1

Question 6 (25 marks)

Question 6 (a)

(i) 1.
$$I_1 = \frac{1}{4}x^4 + x^3 + 3x + 1$$

2.
$$I_2 = \frac{1}{4}x^4 + x^3 + 3x + 2$$

3.
$$I_3 = \frac{1}{4}x^4 + x^3 + 3x + 3$$

FORMULAE AND TABLES BOOK Calculus: Integrals [page 26]

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + c, \ n \neq -1$$

(ii)
$$\int f(x) dx = h(x)$$

h(x) is an indefinite integral which means that when you differentiate it with respect to x you get h(x)

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$$h'(x) = f(x)$$
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(iii)
$$I = \frac{1}{4}x^4 + x^3 + 3x + c$$

Question 6 (b)

(i)
$$h(x) = x \ln x$$

$$h'(x) = x \times \frac{1}{x} + (\ln x) \times 1 = 1 + \ln x$$

(ii) $h'(x) = 1 + \ln x \Rightarrow \ln x = h'(x) - 1$ $\int \ln x \, dx = \int (h'(x) - 1) \, dx = h(x) - x + c = x \ln x - x + c$

FORMULAE AND TABLES BOOK Calculus: Product rule [page 25]

$$y = uv \Rightarrow \frac{dy}{dx} = u\frac{dv}{dx} + v\frac{du}{dx}$$

FORMULAE AND TABLES BOOK Calculus: Derivatives [page 25]

$$y = \ln x \Rightarrow \frac{dy}{dx} = \frac{1}{x}$$